

“Mathematical Modelling of Myeloproliferative Neoplasms and Hematopoietic Stem Cells”

Ph.D.-defense

Rasmus Kristoffer Pedersen

IMFUFA, Department of Science and Environment
Roskilde University, Denmark

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Overall plan: Guided tour of the thesis

- Background on mathematical modelling and blood cancers

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- ▶ Background on mathematical modelling and blood cancers
- ▶ Three particular mathematical models

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- ▶ Background on mathematical modelling and blood cancers
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 - ▶ The combined “HSC-Niche + Cancitis” model

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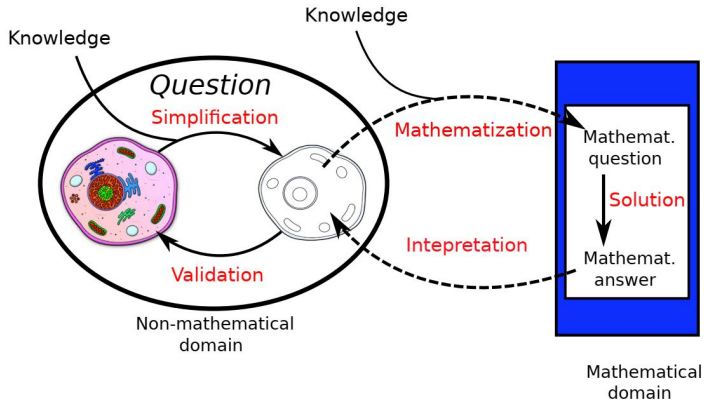
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- ▶ Background on mathematical modelling and blood cancers
- ▶ Three particular mathematical models
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 - ▶ The combined “HSC-Niche + Cancitis” model
- ▶ Comments about mathematical modelling of blood cancers

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The modelling cycle, taken from (Hansen & Ottesen, 2020)

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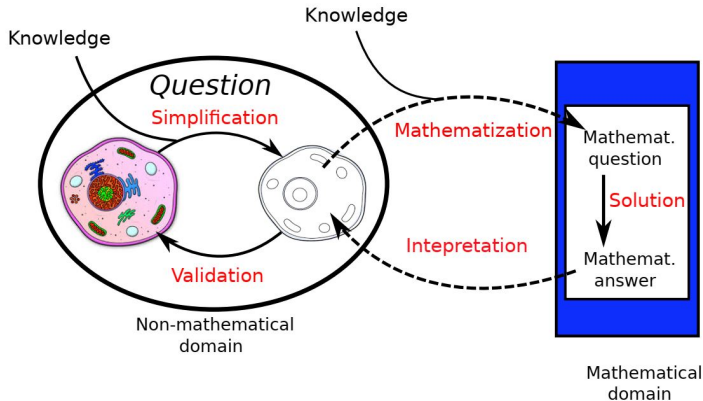
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Mathematical Modelling



The modelling cycle, taken from (Hansen & Ottesen, 2020)

“If you want to be successful, pick a cancer and work on that”

- Doron Levy (University of Maryland), CIRM Math-Cancer workshop, summer 2018

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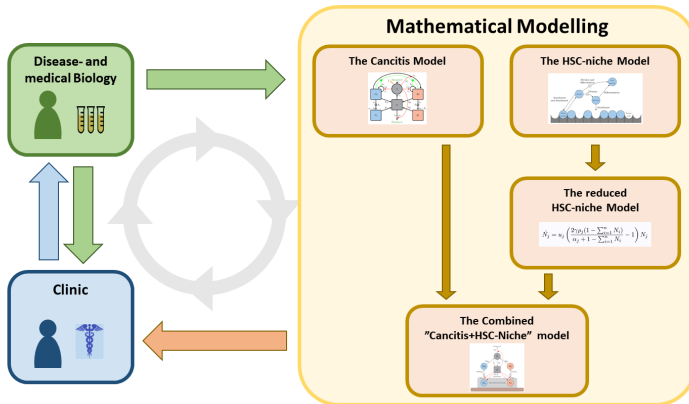
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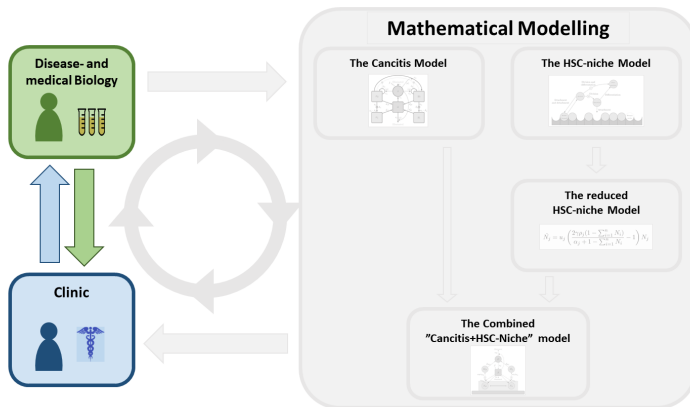
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The blood system and MPNs

- **HSC:** Hematopoietic Stem Cells. Produces progenitor cells.



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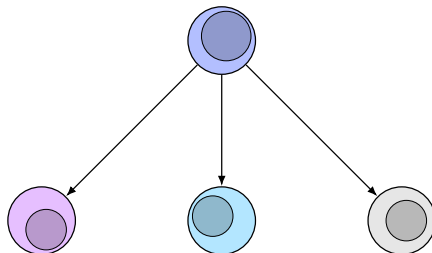
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The blood system and MPNs

- ▶ **HSC:** Hematopoietic Stem Cells. Produces progenitor cells.
- ▶ **Progenitors:** Produces blood cells.



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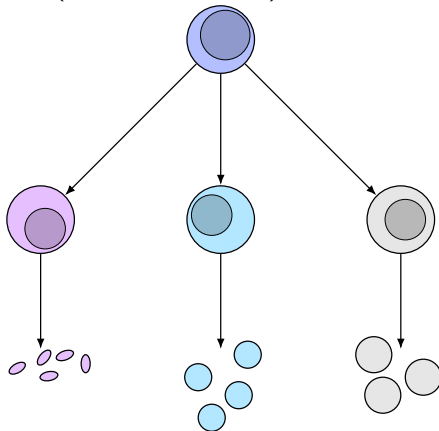
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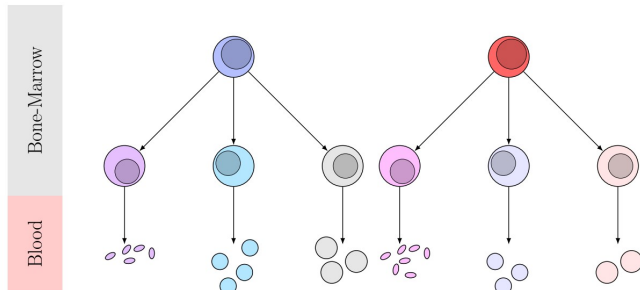
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- ▶ **MPNs:** Myeloproliferative Neoplasms
Group of diagnoses, e.g.
 - ▶ Essential Thrombocythemia (ET)
 - ▶ Polycythemia Vera (PV)
 - ▶ Primary Myelofibrosis (PMF)

Characterised by positive $JAK2^{V617F}$ mutation and heightened blood-cell counts.

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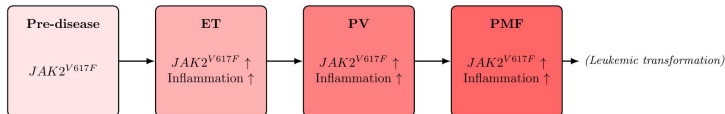
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Characterised by positive $JAK2^{V617F}$ mutation and heightened blood-cell counts.

(Note: We do not consider CML, and focus only on the Philadelphia-chromosome-negative MPNs)

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- Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)

The DALIAH trial

- ▶ Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)
- ▶ \approx 200 Danish MPN patients

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- ▶ Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)
- ▶ ≈ 200 Danish MPN patients
- ▶ 63 with IFN mono-treatment through whole study

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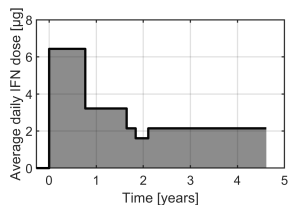
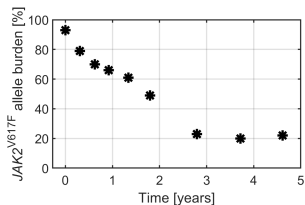
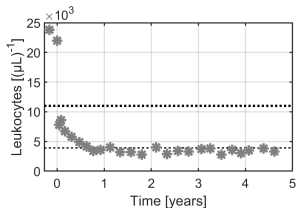
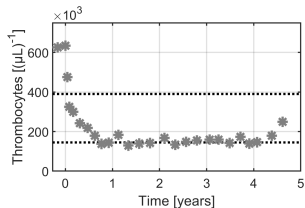
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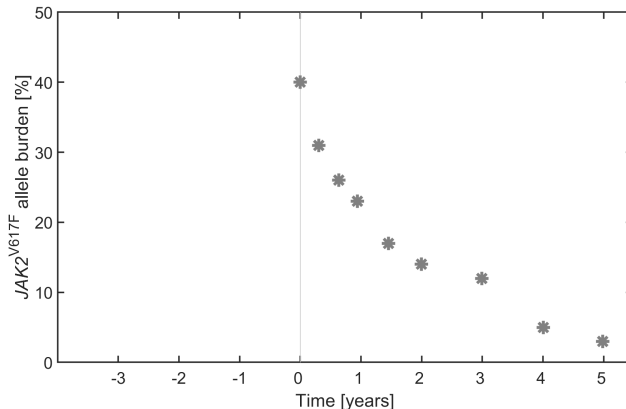
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For details, see chapter 3 or Pedersen et al (2020)

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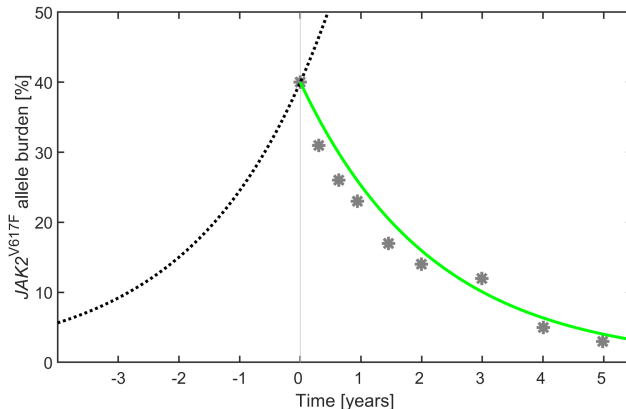
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Comments on empirical approach

- The “what”, not the “why”

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- ▶ The “what”, not the “why”
- ▶ Blood-cells are not considered

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Comments on empirical approach

- ▶ The “what”, not the “why”
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- ▶ Standard-of-care vs. actual IFN-dose

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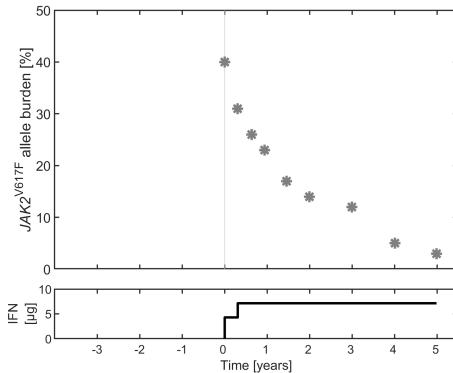
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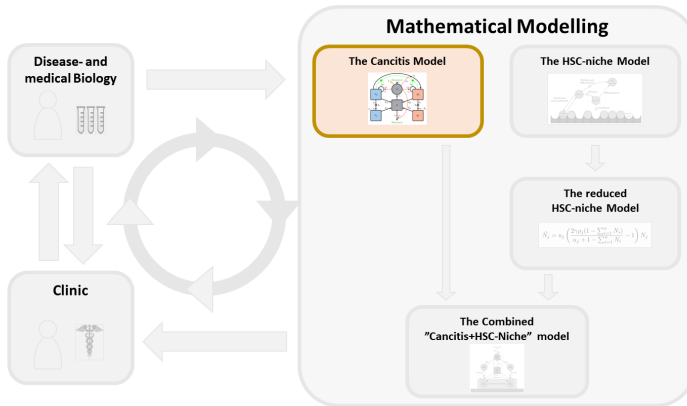
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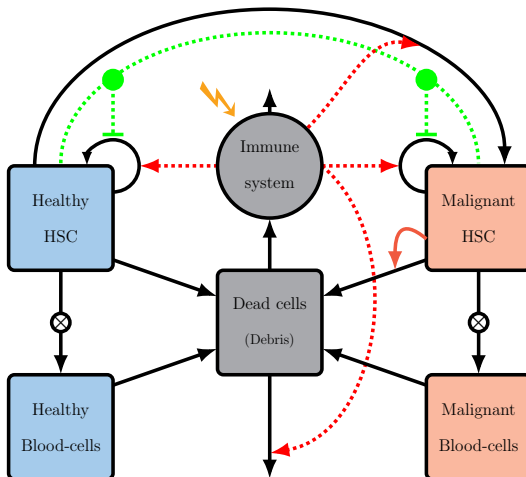
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The Cancitis Model, model description



For details, see chapter 5, figure 5.1 or Andersen et al (2017)

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The Cancitis Model, equations and example

$$\dot{x}_0 = (r_x \phi_x(x_0, y_0)s - d_{x_0} - a_x)x_0 - r_m s x_0$$

$$\dot{y}_0 = (r_y \phi_y(x_0, y_0)s - \hat{d}_{y_0} - \tilde{d}_{y_0} y_0 - a_y)y_0 + r_m s x_0$$

$$\dot{x}_1 = a_x A_x x_0 - d_{x_1} x_1$$

$$\dot{y}_1 = a_y A_y y_0 - d_{y_1} y_1$$

$$\dot{a} = d_{x_0} x_0 + d_{x_1} x_1 + (\hat{d}_{y_0} + \tilde{d}_{y_0} y_0)y_0 + d_{y_1} y_1 - e_a a s$$

$$\dot{s} = r_s a - e_s s + I$$

where $\dot{}$ denotes the time-derivative. The functions $\phi_x(x_0, y_0)$ and $\phi_y(x_0, y_0)$ are defined as:

$$\phi_x(x_0, y_0) = \frac{1}{1 + c_{xx}x_0 + c_{xy}y_0}$$

$$\phi_y(x_0, y_0) = \frac{1}{1 + c_{yx}x_0 + c_{yy}y_0}$$

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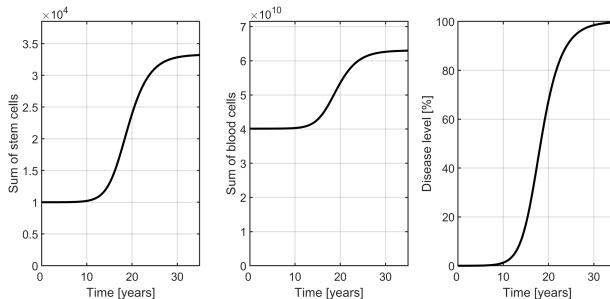
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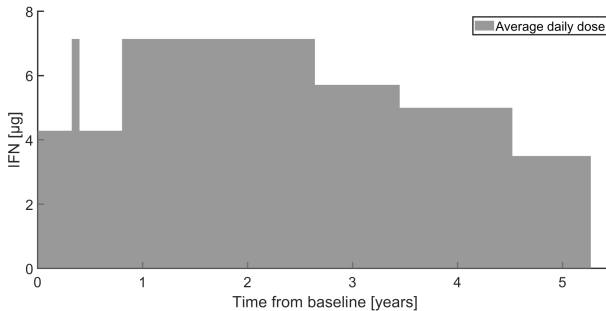
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What happens when the drug is injected?



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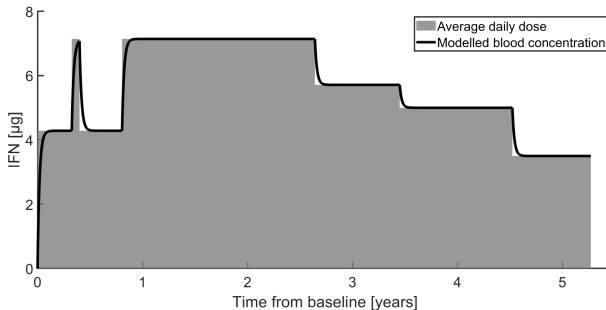
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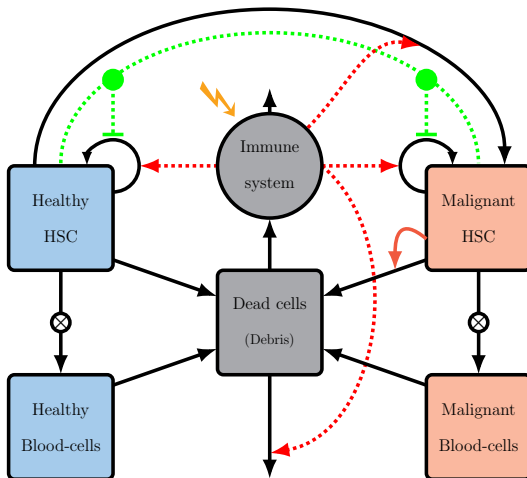
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What happens when the drug is injected?



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What does the drug do?



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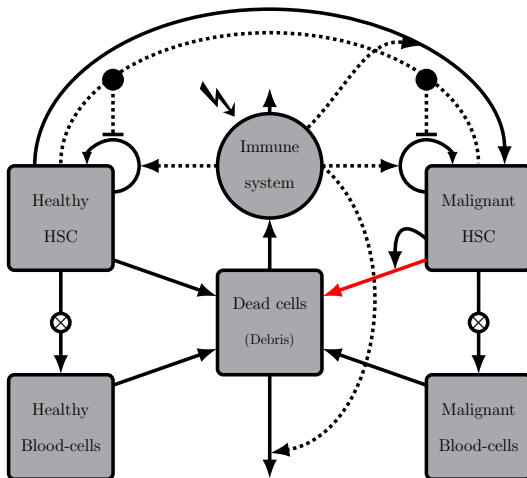
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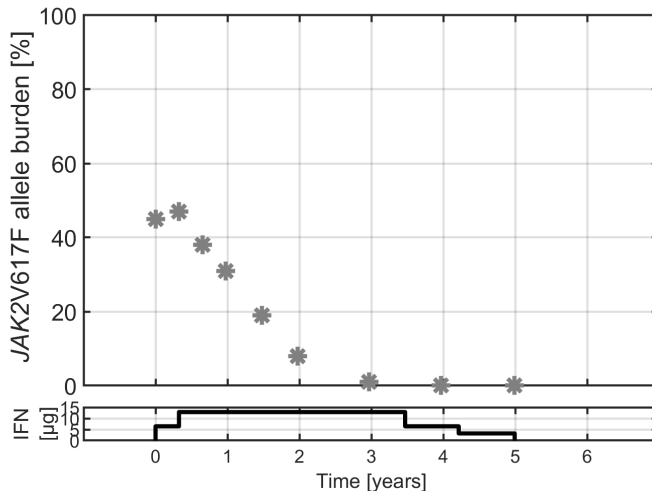
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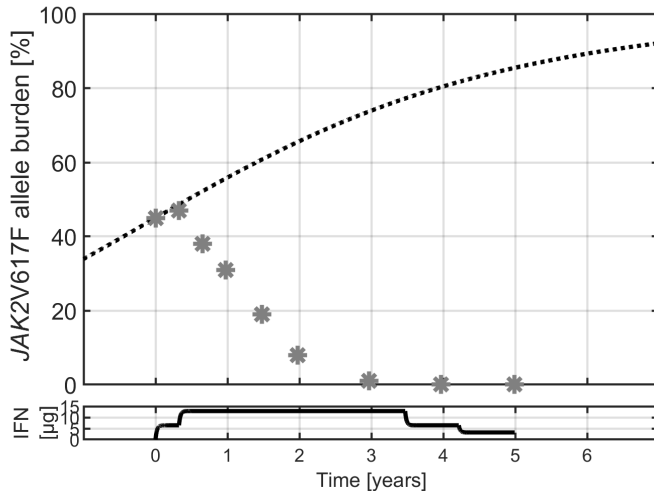
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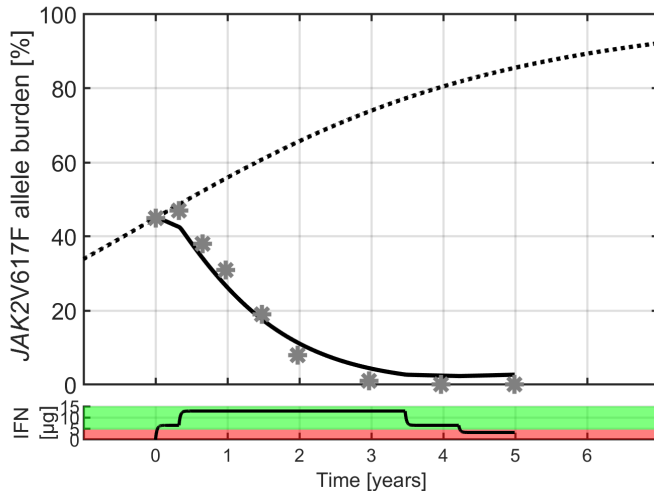
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The Cancitis Model, findings so far

- IFN-induced death of malignant stem cells appears a reasonable hypothesis.

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The Cancitis Model, findings so far

- ▶ IFN-induced death of malignant stem cells appears a reasonable hypothesis.
- ▶ 80% increased death of malignant stem cells causes steady state stability to change, leading to long-term healthy of the patient.

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The Cancitis Model, findings so far

- ▶ IFN-induced death of malignant stem cells appears a reasonable hypothesis.
- ▶ 80% increased death of malignant stem cells causes steady state stability to change, leading to long-term healthy of the patient.
- ▶ For many of the DALIAH patients, this was attained with $5\mu g$ IFN daily ($35\mu g$ weekly)

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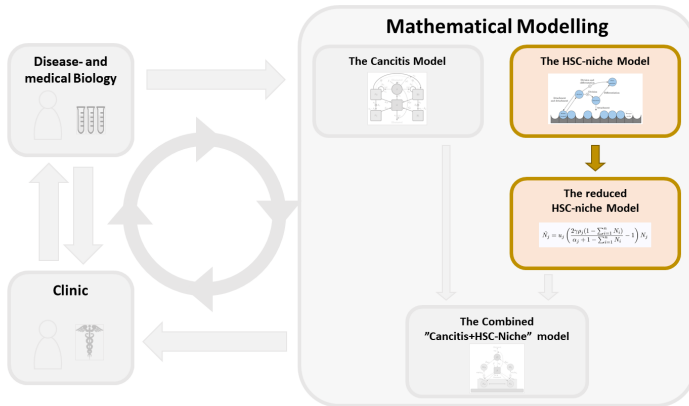
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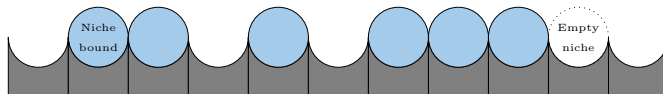
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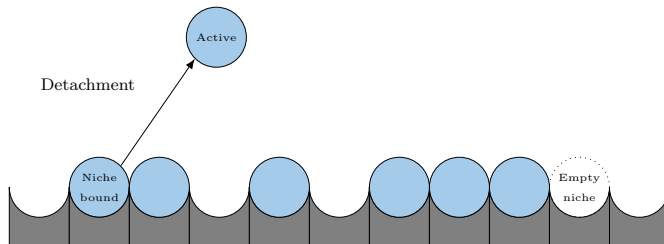
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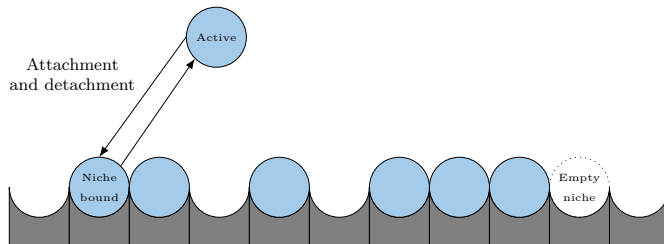
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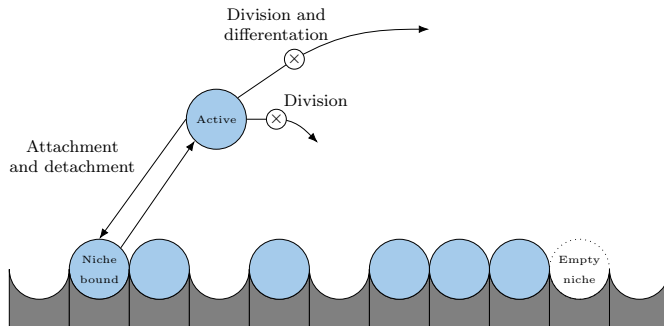
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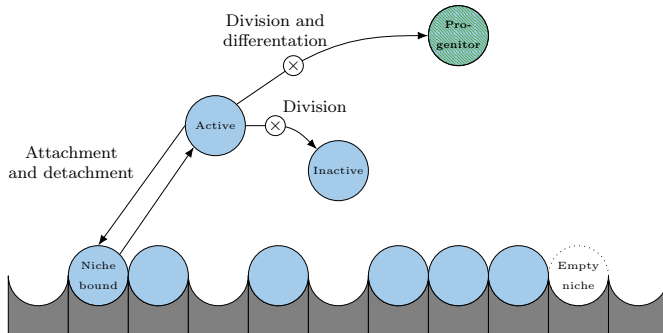
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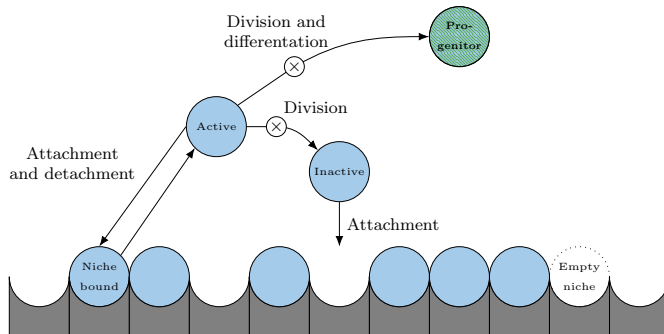
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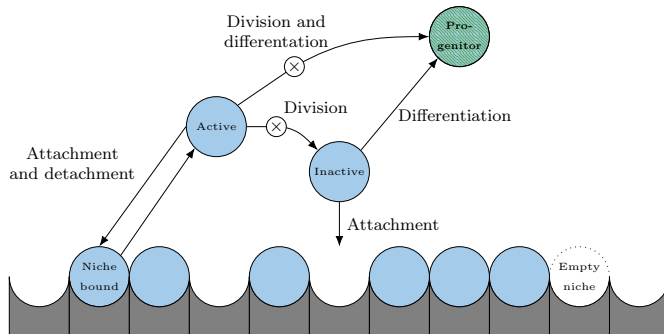
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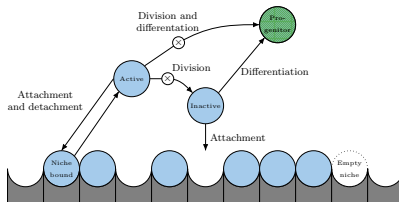
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$$\dot{N} = b_I(K - N)I + b_A(K - N)A - uN$$

$$\dot{I} = 2\gamma rA - b_I(K - N)I - d_I I$$

$$\dot{A} = uN - b_A(K - N)A - rA - d_A A$$

$$N_E = K - N$$

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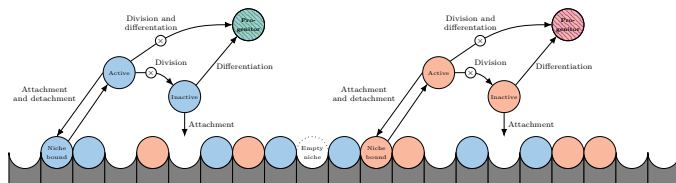
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$$\dot{N}_j = b_{lj} \left(K - \sum_{i=1}^n N_i \right) l_j + b_{Aj} \left(K - \sum_{i=1}^n N_i \right) A_j - u_j N_j$$

$$\dot{l}_j = 2\gamma r_j A_j - b_{lj} \left(K - \sum_{i=1}^n N_i \right) l_j - d_{lj} l_j$$

$$\dot{A}_j = u_j N_j - b_{Aj} \left(K - \sum_{i=1}^n N_i \right) A_j - r_j A_j - d_{Aj} A_j$$

$$N_E = K - \sum_{i=1}^n N_i$$

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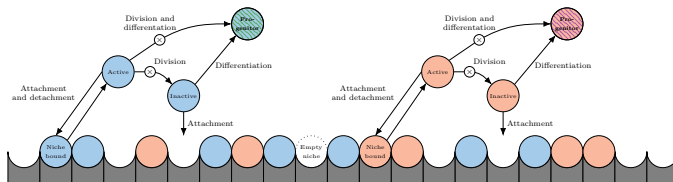
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Malignant

Healthy

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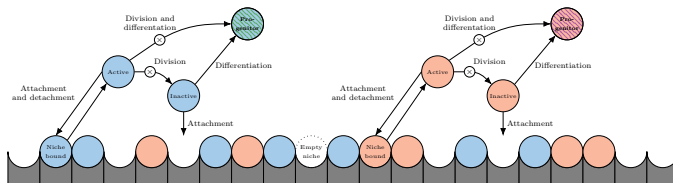
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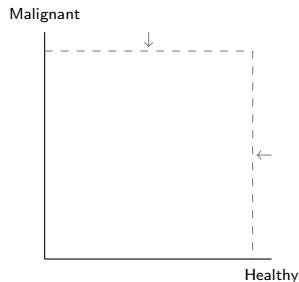
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- ▶ Attractive trapping region



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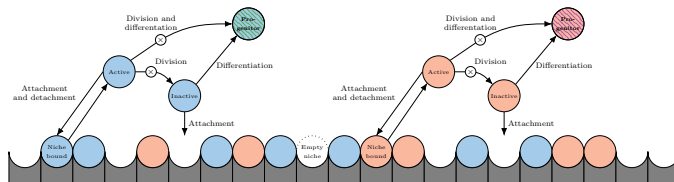
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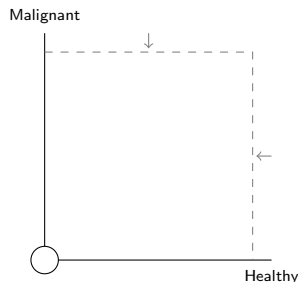
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- Attractive trapping region
- Steady states:
 - No cells (Exhaustion)



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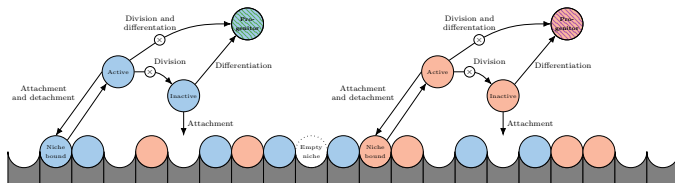
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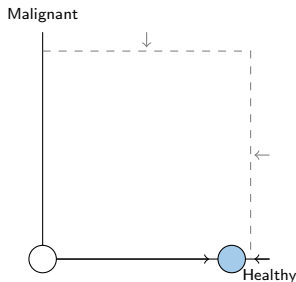
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- Attractive trapping region
- Steady states:
 - No cells (Exhaustion)
 - Only healthy



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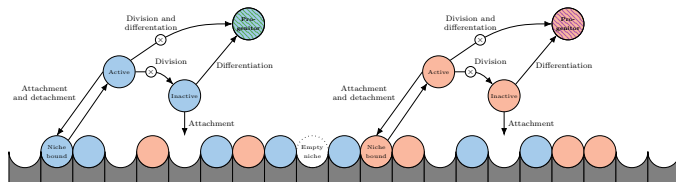
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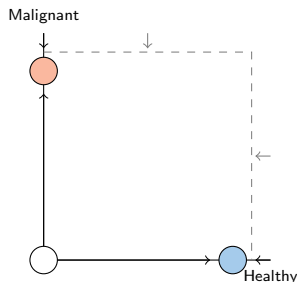
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- Attractive trapping region
- Steady states:
 - No cells (Exhaustion)
 - Only healthy
 - Only malignant



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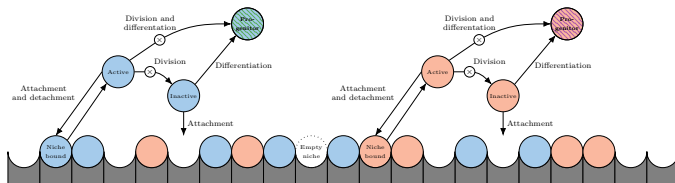
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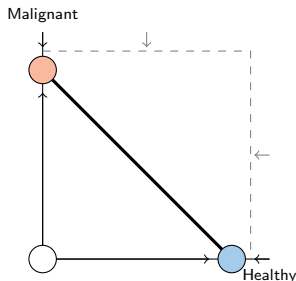
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► Attractive trapping region

► Steady states:

- No cells (Exhaustion)
- Only healthy
- Only malignant
- Co-existence



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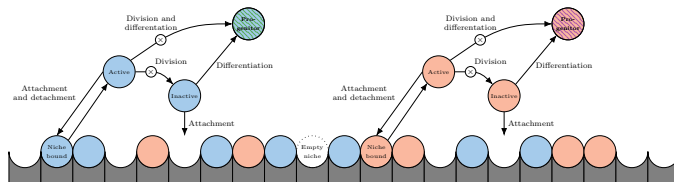
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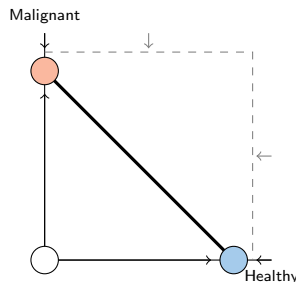
► Attractive trapping region

► Steady states:

- No cells (Exhaustion)
- Only healthy
- Only malignant
- Co-existence

► HSC fitness:

$$F_j = \frac{b_{lj} ((2\gamma - 1)r_j - d_{A_j})}{d_{lj}(r_j + d_{A_j})}$$



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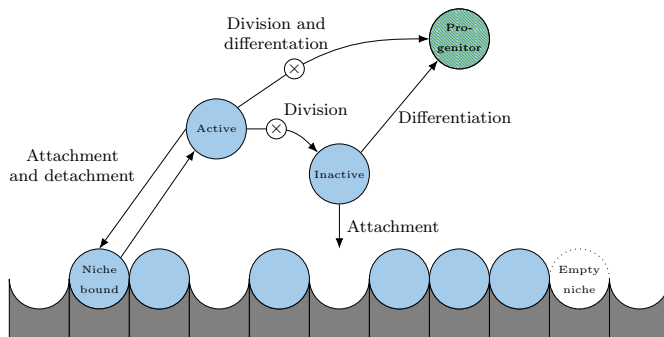
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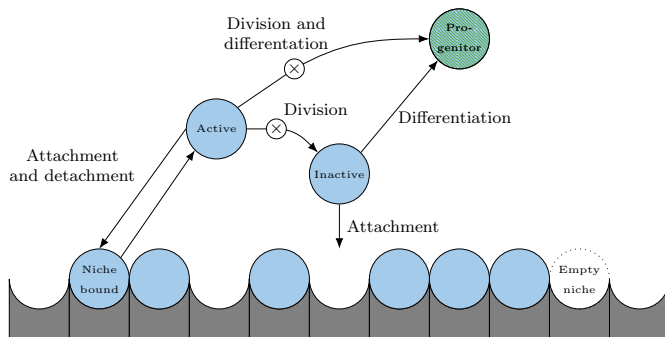
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► **Assumption** Most HSC niches are occupied

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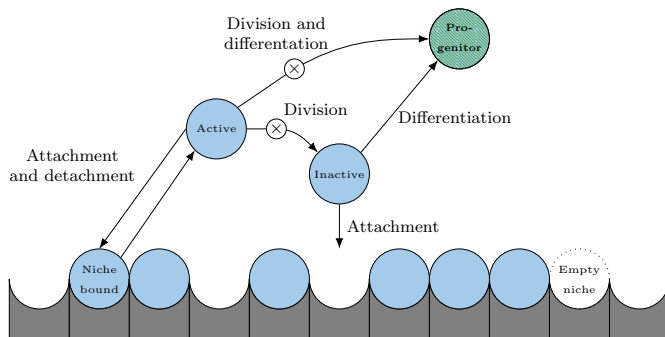
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- **Assumption** Most HSC niches are occupied
- **Assumption** Most HSCs are niche-bound

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- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.

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The HSC niche Model, reduction

- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.
- ▶ Only three parameters per HSC-type: ρ , α and u

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The HSC niche Model, reduction

- **Assumption** Most HSC niches are occupied
- **Assumption** Most HSCs are niche-bound

Consequences:

- No need to keep track of free HSC.
- Only three parameters per HSC-type: ρ , α and u
-

$$\dot{N}_j = u_j \left(\frac{2\gamma\rho_j(1 - \sum_{i=1}^n N_i)}{\alpha_j + 1 - \sum_{i=1}^n N_i} - 1 \right) N_j$$

where $\rho_j = \frac{r_j}{r_j + d_{A_j}}$ and $\alpha_j = \frac{d_{I_j}}{b_{I_j}K}$.

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The HSC niche Model, reduction

- **Assumption** Most HSC niches are occupied
- **Assumption** Most HSCs are niche-bound

Consequences:

- No need to keep track of free HSC.
- Only three parameters per HSC-type: ρ , α and u
-

$$\dot{N}_j = u_j \left(\frac{2\gamma\rho_j(1 - \sum_{i=1}^n N_i)}{\alpha_j + 1 - \sum_{i=1}^n N_i} - 1 \right) N_j$$

where $\rho_j = \frac{r_j}{r_j + d_{A_j}}$ and $\alpha_j = \frac{d_{I_j}}{b_{I_j}K}$.

- Only minor changes to dynamics.

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The HSC niche Model, reduction

- **Assumption** Most HSC niches are occupied
- **Assumption** Most HSCs are niche-bound

Consequences:

- No need to keep track of free HSC.
- Only three parameters per HSC-type: ρ , α and u
-

$$\dot{N}_j = u_j \left(\frac{2\gamma\rho_j(1 - \sum_{i=1}^n N_i)}{\alpha_j + 1 - \sum_{i=1}^n N_i} - 1 \right) N_j$$

where $\rho_j = \frac{r_j}{r_j + d_{A_j}}$ and $\alpha_j = \frac{d_{I_j}}{b_{I_j}K}$.

- Only minor changes to dynamics.
- *Importantly, concept of HSC fitness still exists:*

$$f_j = \frac{2\gamma\rho_j - 1}{\alpha_j}$$

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If there are only two types of HSC, and they are very similar ($f_1 \approx f_2$), we can reduce further.

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If there are only two types of HSC, and they are very similar ($f_1 \approx f_2$), we can reduce further.

$$\dot{C} = \phi(1 - C)C \quad (1)$$

$$\text{where } \phi = g_2(T_1^*) = u_2 \frac{\alpha_2}{\alpha_2 + f_1^{-1}} \left(\frac{f_2}{f_1} - 1 \right).$$

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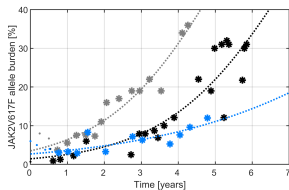
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$$\dot{C} = \phi(1 - C)C \quad (1)$$



(a)

$$\phi > 0$$

$$f_1 < f_2$$

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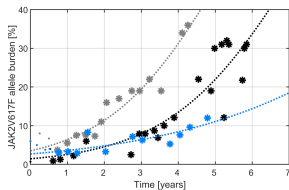
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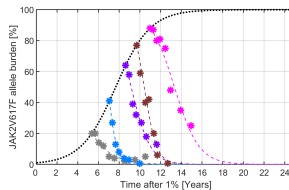
$$\dot{C} = \phi(1 - C)C \quad (1)$$



(a)

$$\phi > 0$$

$$f_1 < f_2$$



(b)

$$\phi < 0$$

$$f_1 > f_2$$

The HSC niche model, summing it up

- A detailed description of an experimentally inaccessible system

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- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises

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The HSC niche model, summing it up

- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises
- ▶ Biologically-grounded simplifications results in a simple logistic expression.

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The HSC niche model, summing it up

- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises
- ▶ Biologically-grounded simplifications results in a simple logistic expression.

Similar to the empirical modelling of the DALIAH trial data!

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The HSC niche model, summing it up

- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises
- ▶ Biologically-grounded simplifications results in a simple logistic expression.
Similar to the empirical modelling of the DALIAH trial data!
- ▶ Possible explanation for *why* data looks the way it does

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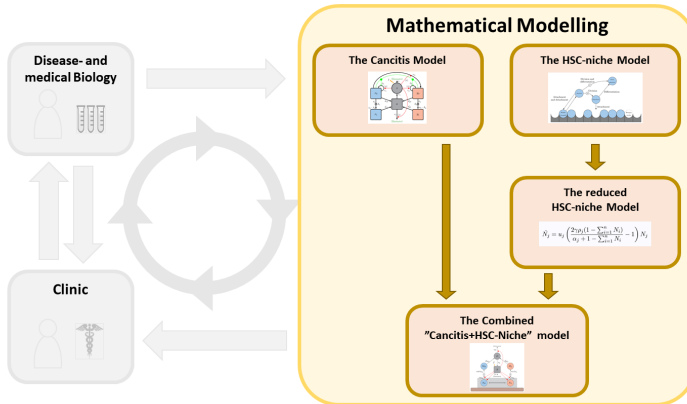
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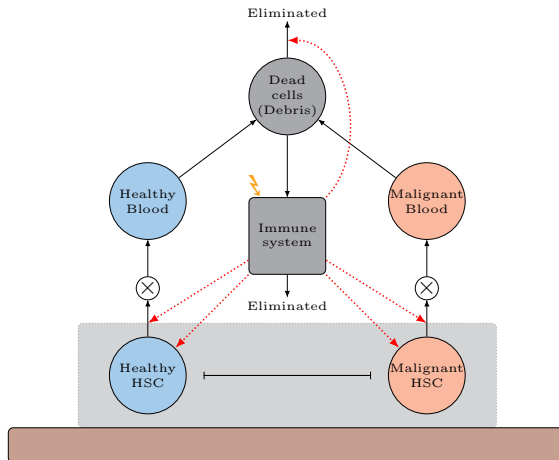
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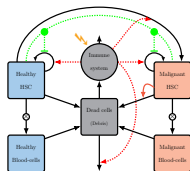
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The combined Cancitis-niche Model



$$\dot{x}_0 = (r_x \phi_x(x_0, y_0)s - d_{x_0} - a_x)x_0 - r_m s x_0$$

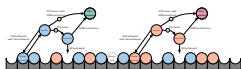
$$\dot{y}_0 = (r_y \phi_y(x_0, y_0)s - \hat{d}_{y_0} - \tilde{d}_{y_0} y_0 - a_y)y_0 + r_m s x_0$$

$$\dot{x}_1 = a_x A_x x_0 - d_{x_1} x_1$$

$$\dot{y}_1 = a_y A_y y_0 - d_{y_1} y_1$$

$$\dot{a} = d_{x_0} x_0 + d_{x_1} x_1 + (\hat{d}_{y_0} + \tilde{d}_{y_0} y_0)y_0 + d_{y_1} y_1 - e_a a$$

$$\dot{s} = r_s a - e_s s + I$$



$$\dot{N}_H = u_H \left(\frac{2\gamma \rho_H (1 - N_H - N_L)}{\alpha_H + 1 - N_H - N_L} - 1 \right) N_H$$

$$\dot{N}_L = u_L \left(\frac{2\gamma \rho_L (1 - N_H - N_L)}{\alpha_L + 1 - N_H - N_L} - 1 \right) N_L$$

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$$\dot{N}_H = u_H S \left(\frac{2\gamma\rho_H(1 - N_H - N_L)}{\alpha_H + 1 - N_H - N_L} - 1 \right) N_H$$

$$\dot{N}_L = u_L S \left(\frac{2\gamma\rho_L(1 - N_H - N_L)}{\alpha_L + 1 - N_H - N_L} - 1 \right) N_L$$

$$\dot{M}_H = \omega_H i_{D_H} S - d_{M_H} M_H$$

$$\dot{M}_L = \omega_L i_{D_L} S - d_{M_L} M_L$$

$$\dot{D} = d_{M_H} M_H + d_{M_L} M_L - e_D D S$$

$$\dot{S} = r_S D - e_S S + I$$

Purple: Cancitis model, green: HSC-Niche model

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$$\dot{N}_H = u_H S \left(\frac{2\gamma\rho_H(1 - N_H - N_L)}{\alpha_H + 1 - N_H - N_L} - 1 \right) N_H$$

$$\dot{N}_L = u_L S \left(\frac{2\gamma\rho_L(1 - N_H - N_L)}{\alpha_L + 1 - N_H - N_L} - 1 \right) N_L$$

$$\dot{M}_H = \omega_H i_{D_H} S - d_{M_H} M_H$$

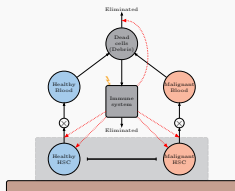
$$\dot{M}_L = \omega_L i_{D_L} S - d_{M_L} M_L$$

$$\dot{D} = d_{M_H} M_H + d_{M_L} M_L - e_D D S$$

$$\dot{S} = r_S D - e_S S + I$$

where $i_{D_j} = \left(2 - 2\rho_j + \frac{2\gamma\alpha_j\rho_j}{\alpha_j + 1 - N_H - N_L} \right) u_j K N_j$. All parameters are non-negative. In addition, $\rho_j \leq 1$ and $\gamma \geq 1$.

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- Feedback from blood to the HSC system: Increases HSC activation

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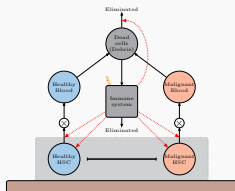
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- Feedback from blood to the HSC system: Increases HSC activation
- A refined description of HSC behaviour

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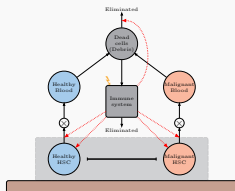
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- Feedback from blood to the HSC system: Increases HSC activation
- A refined description of HSC behaviour
- Same steady states as HSC niche model

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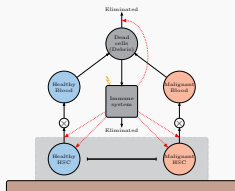
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- Feedback from blood to the HSC system: Increases HSC activation
- A refined description of HSC behaviour
- Same steady states as HSC niche model
 - No cells
 - Single-type steady state

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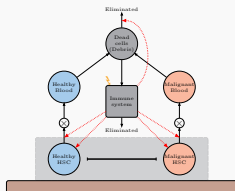
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- ▶ Feedback from blood to the HSC system: Increases HSC activation
- ▶ A refined description of HSC behaviour
- ▶ Same steady states as HSC niche model
 - ▶ No cells
 - ▶ Single-type steady state
 - ▶ Co-existence steady state

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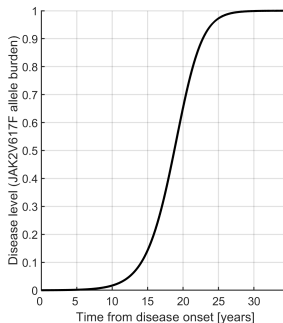
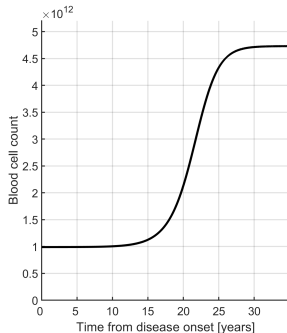
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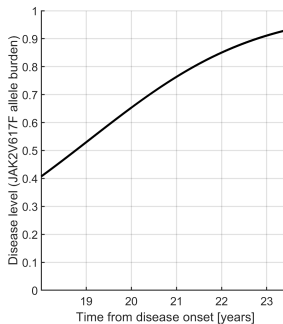
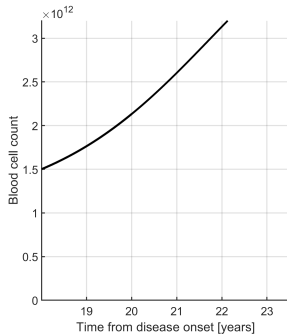
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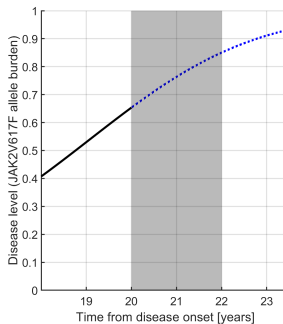
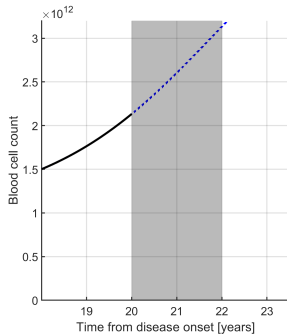
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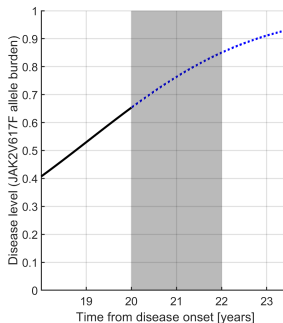
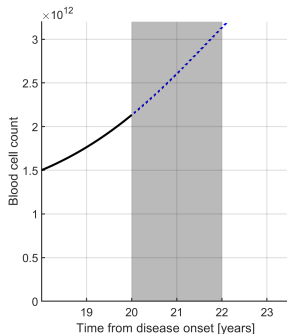
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(For the Cancitis model: Death of HSC)

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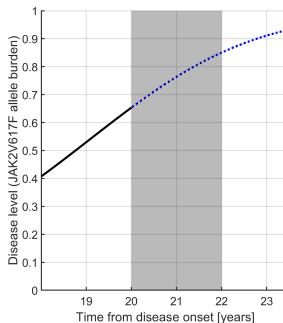
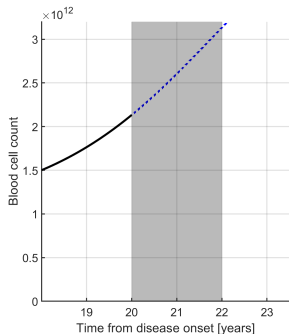
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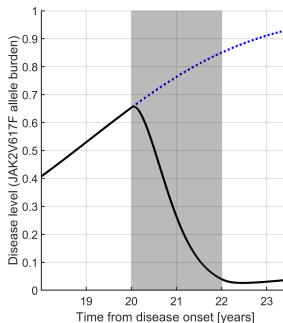
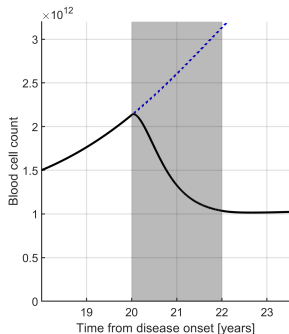
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For the combined model:

- Decreased self-renewal of mutated cells, ρ_L

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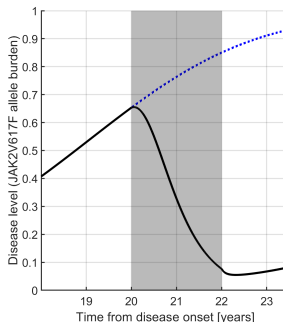
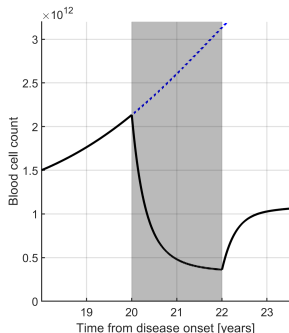
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For the combined model:

- ▶ Decreased self-renewal of mutated cells, ρ_L
- ▶ Death of all actively dividing cells, ω_H and ω_L

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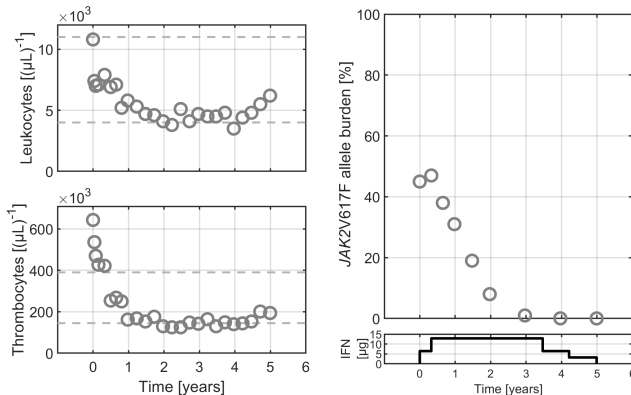
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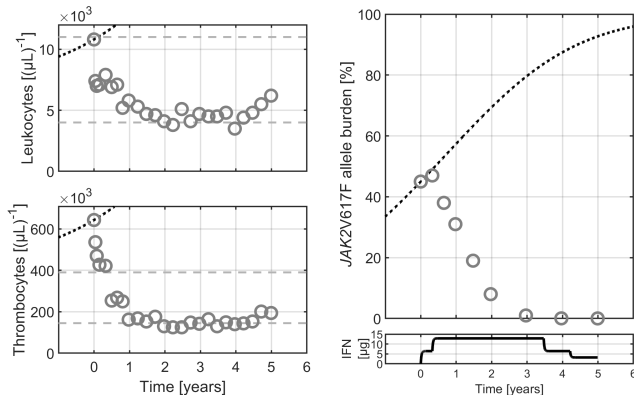
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Patient P198, Data, Growth and PK/PD-modelling

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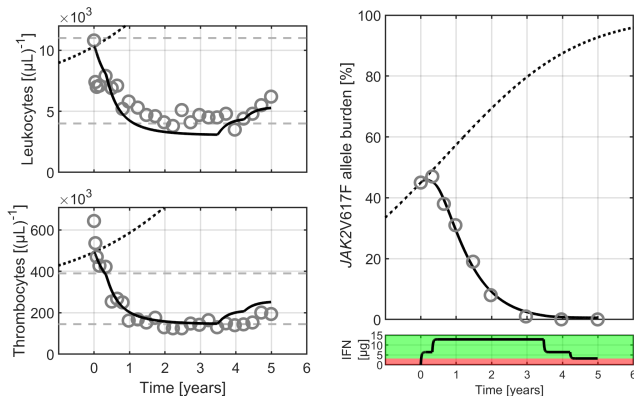
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Patient P198, IFN-dose dependent fitting of model-parameters

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Then what?

Population modelling!

Goal: To describe the effect of IFN on a population level, so expected outcome of treatment can be predicted (with estimated uncertainties of prediction)

Proof-of-concept population modelling

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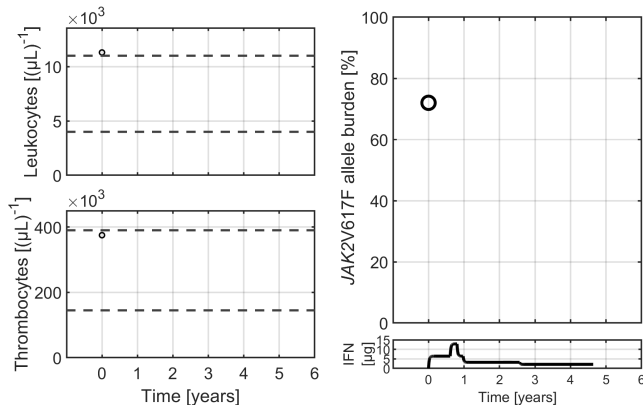
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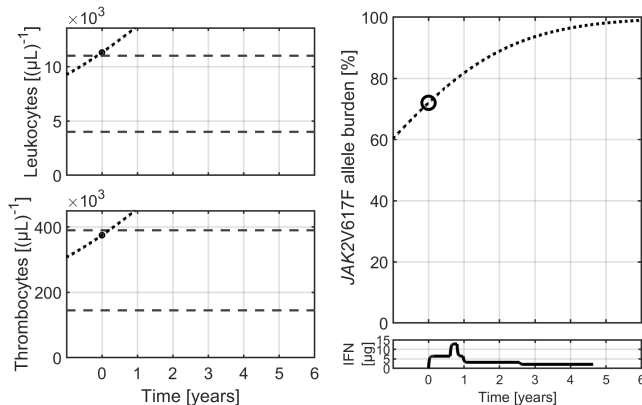
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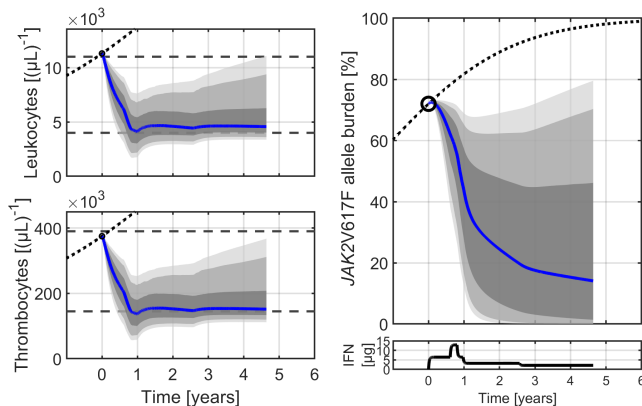
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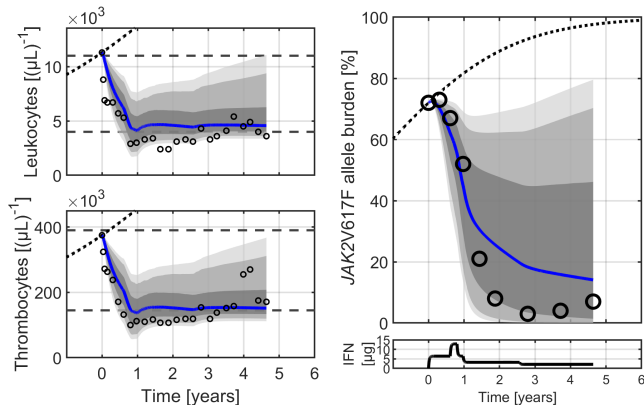
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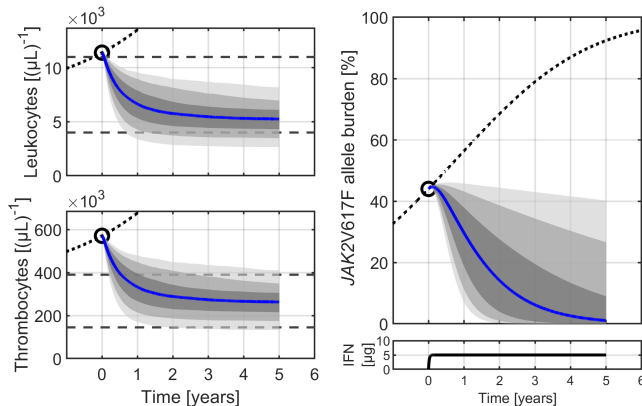
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Patient P082

A hypothetical “typical PV-diagnosed patient”



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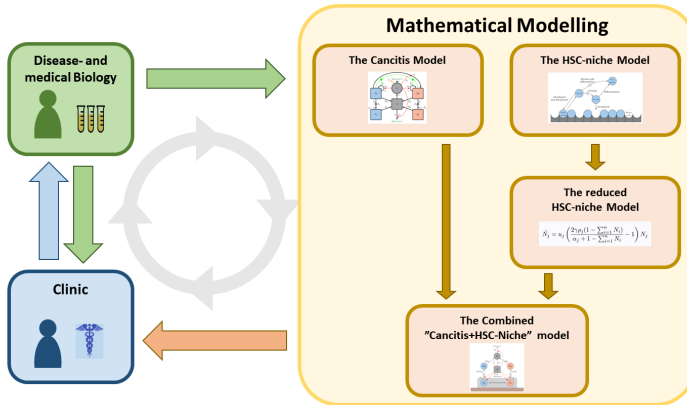
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Through mathematical modelling we have come up with:

- Hypotheses about the behaviour of HSC.

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- ▶ Hypotheses about the behaviour of HSC.
- ▶ Numerical estimates of efficient HSC treatment requires.
- ▶ Biological interpretation of the effect of IFN, on a personalized level.
- ▶ Population-level predictions about the expected response of newly diagnosed MPN patients.

Where to go from here?

- Additional model-validation and data-collection.

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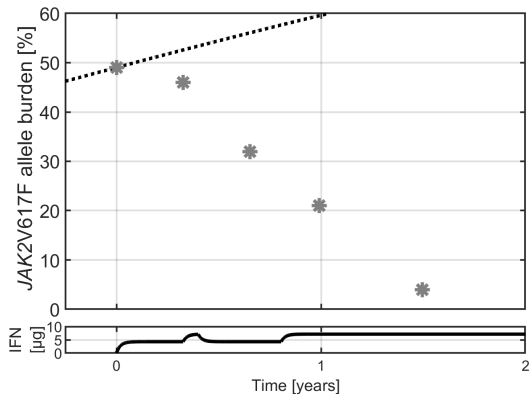
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Where to go from here?

- Additional model-validation and data-collection.

Particularly for the first year of treatment.



Patient P002

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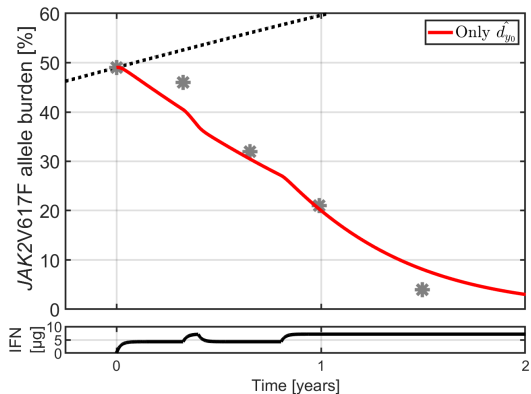
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Where to go from here?

- Additional model-validation and data-collection.

Particularly for the first year of treatment.



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Where to go from here?

- ▶ Additional model-validation and data-collection.
- ▶ Improved identification/stratification of patient sub-diagnoses.

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Where to go from here?

- ▶ Additional model-validation and data-collection.
- ▶ Improved identification/stratification of patient sub-diagnoses.
- ▶ Consideration of other drugs (HU, Ruxo, Jakavi, Statins, etc.), and combination treatment.

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Where to go from here?

- ▶ Additional model-validation and data-collection.
- ▶ Improved identification/stratification of patient sub-diagnoses.
- ▶ Consideration of other drugs (HU, Ruxo, Jakavi, Statins, etc.), and combination treatment.
- ▶ Including additional available data (Cytokine-level, smoking, age, etc.)

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Personalized Mathematical Modelling?

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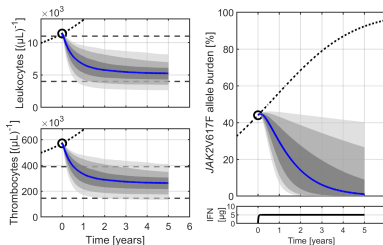
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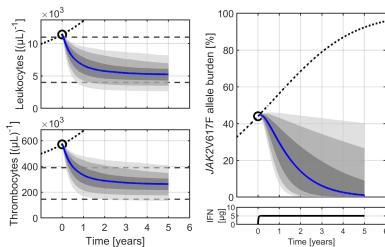
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Is mathematical modelling the primary clinical tool of tomorrow?

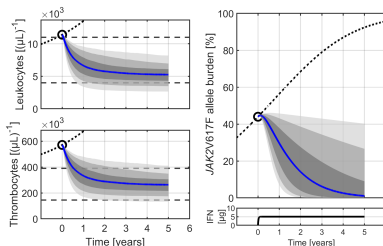


Is mathematical modelling the primary clinical tool of tomorrow?



“Completely irresponsible to let mathematical models make decisions...”

Is mathematical modelling the primary clinical tool of tomorrow?



“Completely irresponsible to let mathematical models make decisions, but even worse to ignore them”
- Johnny T. Ottesen

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Thank you for your time
and attention!

Thank you for your time and attention!

And a big thanks to supervisors and collaborators:

- ▶ Johnny Ottesen, Morten Andersen and Hans Hasselbalch
- ▶ Thomas Stiehl
- ▶ Johanne Gudmand-Høyer, Zamra Sajid and Marc Dam
- ▶ Vibe Skov, Lasse Kjær and Trine Knudsen

Extra slides and figures

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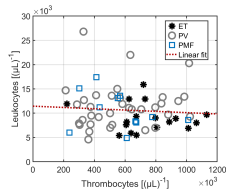
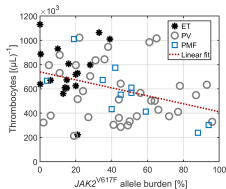
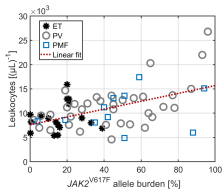
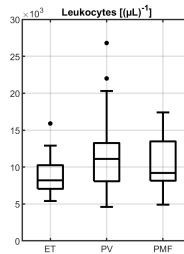
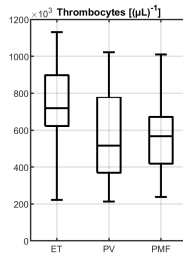
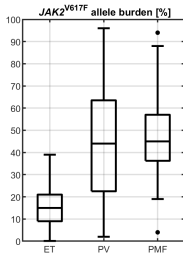
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The framework of Brady & Enderling (2019)

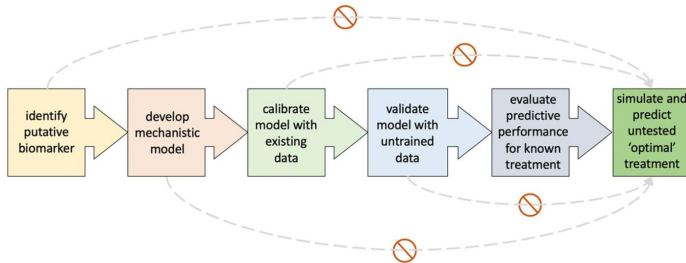


Figure from Brady & Enderling (2019)

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The effect of IFN, “hypothetical” consequences

Assuming our guess of the IFN-effect is valid

($\rho_L \downarrow$, $\omega_H \downarrow$ and $\omega_L \downarrow$)

What are the consequences?

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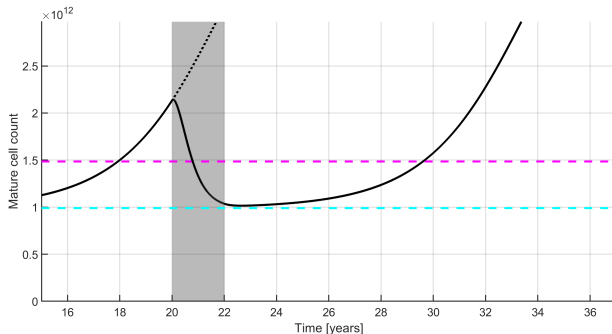
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The effect of IFN, “hypothetical” consequences

Assuming our guess of the IFN-effect is valid

($\rho_L \downarrow$, $\omega_H \downarrow$ and $\omega_L \downarrow$)

What are the consequences?



(Here, only ρ_L was decreased)

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